

Inverter application manual

Energy-saving effect with inverter driving for the control of Fans and pumps

Toshiba Schneider Inverter Corporation

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1. Introduction

- Why does a motor drive with inverter allow energy saving?

The damper is used for lowering the air capacity or flow of the fans or pumps operated at a constant speed.

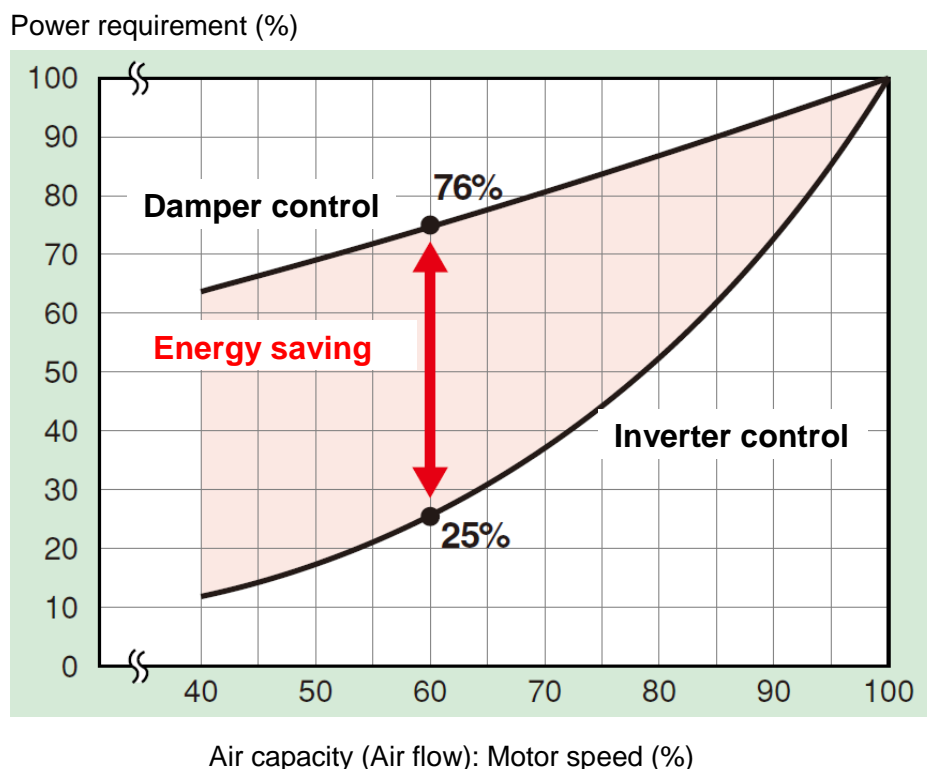
In this case, because of commercial operation, the speed of motor is constant. Therefore, the motor power does not change so much as curve ①, relative to the load variation due to controlled damper.

On the other hand, when the speed is decreased in order to reduce the air capacity or flow of fans or pumps, the motor power will extremely drop because it is ideally in proportion to the cube of speed as described in item ②.

Therefore, the output can be lowered to the minimal level by controlling the speed with inverter drive.

For the energy-saving effect, the greater the variation of air capacity or flow becomes the larger effect it is expectable to have. However, there is no effect with a constant or slightly-changed (approx. 95~100%) air capacity or flow.

Relation between the air capacity or flow and the power
(in case of speed control)



Note) The upper figure shows power requirement. It is necessary to consider efficiency.

2. Energy-saving effect due to flow and pressure control

Fig. 1 is a graph of relation between pump flow Q and discharge pressure (head) H , Q - H characteristic. H_{n1} is a characteristic curve at the rated speed. Node A with duct resistance curve $R1$ indicates the rated capacity.

(Rated discharge pressure-equivalent flow: Q_a)

While the duct resistance increases almost in proportion to the square of flow Q with real head H_s as reference, it is also raised by stopping down a damper on the discharge side ($R1 \rightarrow R2$).

Pump shall be operated at the node between these two curves: pump characteristic curve and duct resistance curve.

In order to decrease the flow from Q_a to Q' , the following procedure shall be performed:

- 1) Flow control by opening/closing the damper

By stopping down the damper to increase the duct resistance curve from $R1$ to $R2$ and move it to node B with characteristic curve H_{n1} , flow Q' will be achieved and the discharge pressure will be raised from H_a to H_b .

- 2) Flow control due to controlled speed

Because the damper is not controlled, the duct resistance is $R1$ only. However, by reducing the speed to decrease the pump characteristic curve from H_{n1} to H_{n2} , node C -equivalent flow Q' will be obtained.

When the flow is lowered from Q_a to Q' , the discharge pressure is simultaneously decreased from H_a to H_c .

[Shaft power difference]

Shaft power difference between the damper control and the control of speed is as shown below:

$$\text{Pump shaft power } P = \frac{K \times Q \times H}{\eta} \quad \text{where, } K: \text{constant; } \eta: \text{pump efficiency}$$

Therefore, the shaft power of the pump being operated at point B in fig. 1 can be obtained as follows:

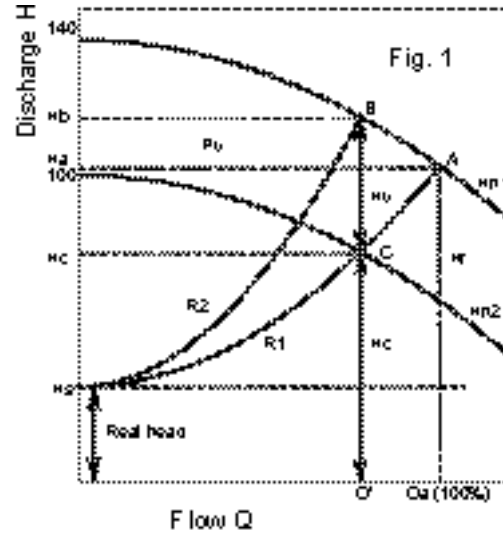
$$P_b = \frac{K \times Q' \times H_b}{\eta} = \frac{K \times Q' \times H_c}{\eta} + \frac{K \times Q' \times H_v}{\eta}$$

The shaft power of the pump being operated at point C can be acquired as follows:

$$P_c = \frac{K \times Q' \times H_c}{\eta}$$

Accordingly, the shaft power difference is calculated as $P_b - P_c = \frac{K \times Q' \times H_v}{\eta}$ and the netted area (P_v)

as shown in fig. 1 indicates the differential shaft power, energy saving.



2.1. Calculation formula (flow control)

Assuming the shut-off pressure to be 140% of rating in fig. 1, this pump characteristic can be expressed in the following formula: $H_p.u = 1.4 - 0.4Q_p.u^2$. P.u: Indication of ratio (per unit)

Similarly, based on the mathematization of duct resistance curve, $R_p.u$ per real head is calculated as follows:

(Respective duct resistance curves are as shown in fig. 2.)

$$a: R_a = Q_p.u^2$$

$$b: R_b = 0.3 + 0.7Q_p.u^2$$

$$c: R_c = 0.6 + 0.4Q_p.u^2$$

Assuming the pump efficiency to be constant, the differential shaft power can be expressed as follows:

$$= P_n \times (H_p.u - R_p.u) Q_p.u$$

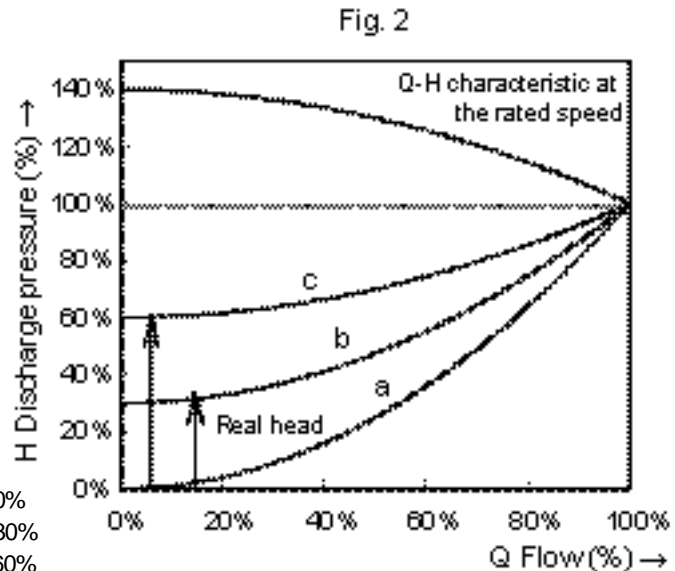
P_n : Rated shaft power (kW)

Assigning expressions to the above equations $H_p.u$ and $R_p.u$, respectively, to be fixed, the differential shaft power, energy saving: P_e , per duct resistance curve relative to flow $Q_p.u$ can be expressed as follows:

$$a: P_e = P_n \times 1.4(1 - Q_p.u^2) \times Q_p.u \text{ (kW)} \quad \text{Real head} = 0\%$$

$$b: P_e = P_n \times 1.1(1 - Q_p.u^2) \times Q_p.u \text{ (kW)} \quad \text{Real head} = 30\%$$

$$c: P_e = P_n \times 0.8(1 - Q_p.u^2) \times Q_p.u \text{ (kW)} \quad \text{Real head} = 60\%$$



* In case of fan blower, curve a shall be used.

P_n : Rated shaft power (kW); $Q_p.u$: Ratio of average engaged capacity to the rated capacity

Real head: Proportion to the rated pressure

With different shut-off pressure or real head, the result can be obtained by assigning values in the following equation:

$$P_e = P_n \times (H_m - H_x)(1 - Q_x^2) \times Q_x \text{ (kW)}$$

H_m : Shut-off pressure (pressure with capacity 0); H_x : Read head; Average capacity

In order to calculate the saved electricity charge, the above-obtained value (kW) shall be multiplied by the annual operating time and the watt-hour rate.

2.2. Calculation formula (pressure control)

With constantly-controlled discharge pressure of pump, by replacing $R_{p.u}$ under flow control with the set pressure $P_{p.u}$ (% to the rated pressure) to assign values of 1, 0.7 and 0.4 in case that the shut-off pressure is 140% of rating, the following equations are obtained. The lower the set pressure gets, the greater the energy-saving effect becomes:

$$P_{p.u}(1) = P_n \times (0.4 - 0.4 Q_{p.u}^2) \times Q_{p.u} (\text{kW})$$

$$P_{p.u}(0.7) = P_n \times (0.7 - 0.4 Q_{p.u}^2) \times Q_{p.u} (\text{kW})$$

$$P_{p.u}(0.4) = P_n \times (1 - 0.4 Q_{p.u}^2) \times Q_{p.u} (\text{kW})$$

With different shut-off pressure or set pressure, the result can be calculated by assigning values to the following equation:

$$P_e = P_n \times \{(H_m - P_x) - (H_m - 1) \times Q_x^2\} \times Q_x (\text{kW})$$

H_m : Shut-off pressure (pressure with flow 0); P_x : Set pressure; Q_x : Average flow

In order to calculate the saved electricity charge, the above-obtained value (kW) shall be multiplied by the annual operating time and the watt-hour rate.

3. Material 3 (calculation formula and data)

1. Speed of motor (min^{-1}) (synchronous speed)

$$= \frac{120 \times \text{Frequency(Hz)}}{P(\text{Number of motor poles})}$$

2. Input electric power (kW) in case of driving with direct commercial power input

$$= \frac{\text{Output capacity of motor (kW)} \times \text{Load factor}}{\text{Motor efficiency}}$$

3. Input electric power (kW) in case of driving with inverter

$$= \frac{\text{Output capacity of motor (kW)}}{\text{Motor efficiency} \times \text{Inverter efficiency}} \times \left(\frac{\text{Revolving speed}}{\text{Rated revolving speed}} \right)^3$$

* Speed = Speed in case of driving with inverter

* Rated speed = Speed of engaged motor in case of driving with direct commercial power supply

4. Shaft power requirement P (kW)

- 1) In case of fan

$$P = \frac{Q \times H \times K}{6120 \times \eta \times 9.81}$$

* Q : Air capacity (m^3/min)

* H : Wind pressure (Pa)

* K : Coefficient

* η : Efficiency (%)

- 2) In case of pump

$$P = \frac{(1.1 \sim 1.2) \times Q \times H \times \gamma}{6.12 \times \eta}$$

* Q : Pump discharge (m^3/min)

* H : Total head (m)

* γ : Mass per unit cubage of fluid (kg/l)

* η : Efficiency (%)

5. Inverter efficiency (%)

90~96% in general: Depends on inverter capacity and model, etc.

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